

DeepSeek-R1 and the Rise of Open Large Reasoning Models

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Research Scientist at Hugging Face

Why train large reasoning models?

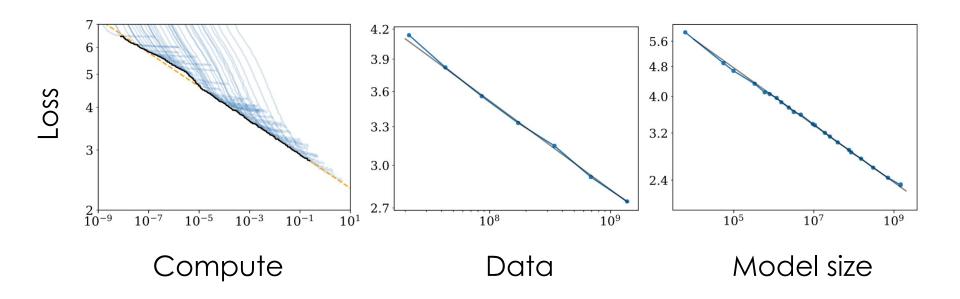
Can we train fully open reasoning models?

What impact has DeepSeek-R1 had on open AI?

Why train large reasoning models?

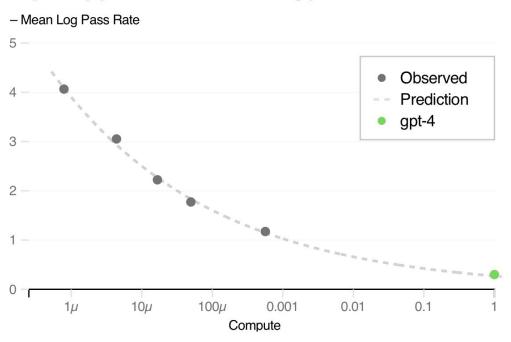
scaling, code, tool-use

Scaling laws: predictable returns



Scaling laws: predictable returns

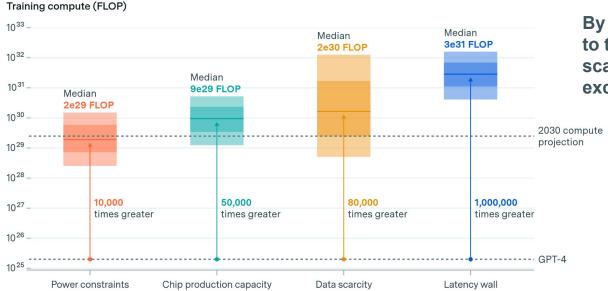
Capability prediction on 23 coding problems



Limits to scaling?

Constraints to scaling training runs by 2030



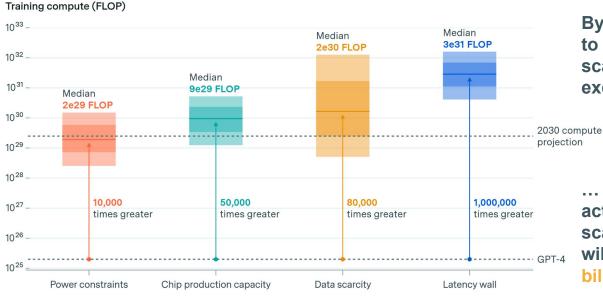


By 2030 it will be very likely *possible* to train models that exceed GPT-4 in scale to the same degree that GPT-4 exceeds GPT-2 in scale ...

Limits to scaling?

Constraints to scaling training runs by 2030





By 2030 it will be very likely *possible* to train models that exceed GPT-4 in scale to the same degree that GPT-4 exceeds GPT-2 in scale ...

... whether AI developers will actually pursue this level of scaling depends on their willingness to invest hundreds of billions of dollars

Limits to scaling?

NewScientist

Is OpenAI hitting a wall with huge and expensive GPT-4.5 model?

Some researchers think OpenAl's giant and expensive latest model is a sign that tech companies cannot keep making progress by continually scaling up

By Matthew Sparkes

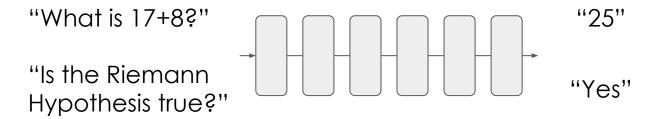
28 February 2025

2025-04-14: GPT-4.5-preview

On April 14th, 2025, we notified developers that the gpt-4.5-preview model is deprecated and will be removed from the API in the coming months.

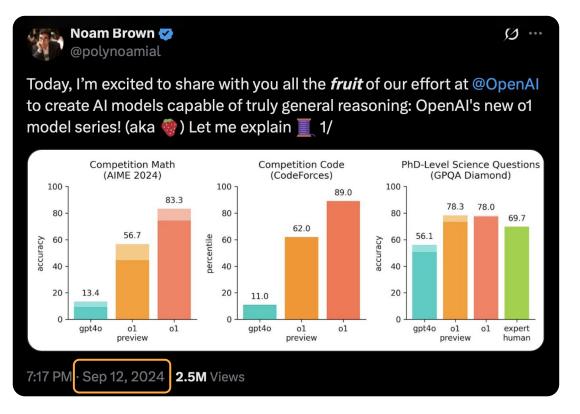
SHUTDOWN DATE	MODEL / SYSTEM	RECOMMENDED REPLACEMENT
2025-07-14	gpt-4.5-preview	gpt-4.1

deprecated less than 2 months after release!

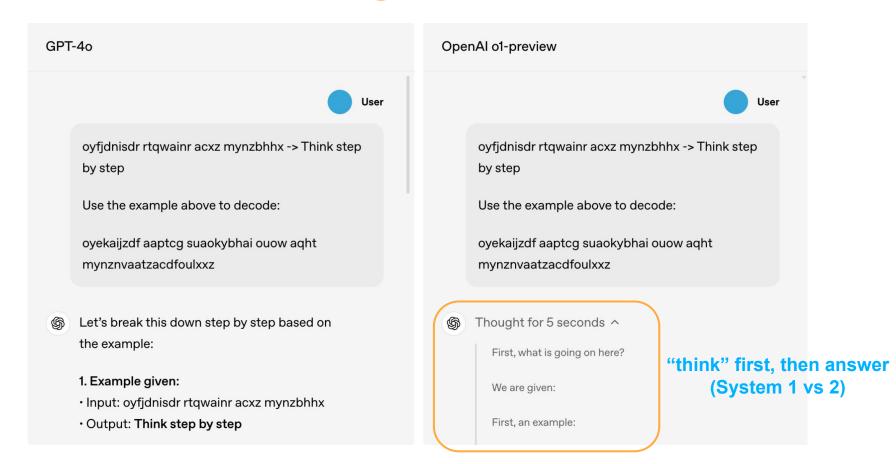


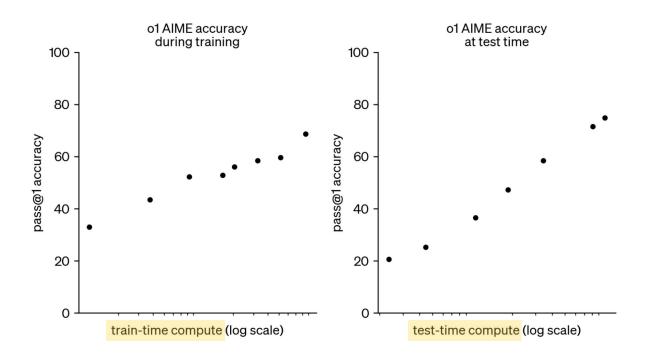
A transformer model uses fixed amount of compute per token irrespective of difficulty.

So how can we scale compute at inference-time?



o1 - the first large reasoning model







ol: what we knew

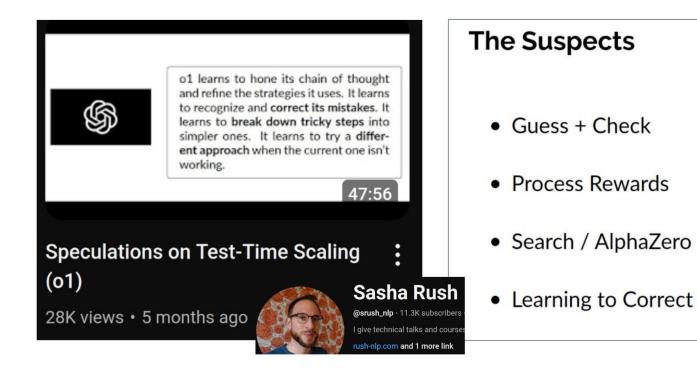
model learns "by itself" search

"Think step by step"

Our large-scale **reinforcement learning** algorithm teaches the model how to think productively using its **chain of thought** in a highly data-efficient training process.

- OpenAI, 2024

o1: how did it actually work?



cs.CL] 22 Jan 2025

DeepSeek-R1: first open-weights reasoner

DeepSeek-R1: Incentivizing Reasoning Capability in LLMs via Reinforcement Learning

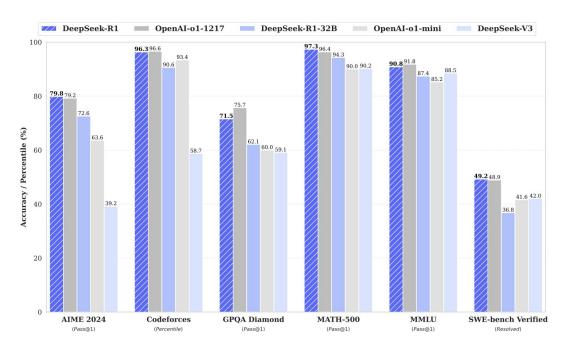


Figure 1 | Benchmark performance of DeepSeek-R1.

~4 months after o1

Models: 8

Downloads: 9.1M

Derivatives: 2.5k

Downloads: 4.4M

last 30 days

https://arxiv.org/abs/2501.12948

DeepSeek-R1: similar to o1

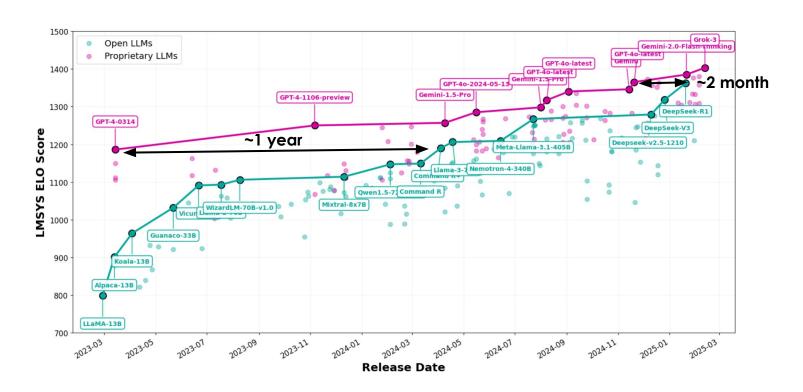




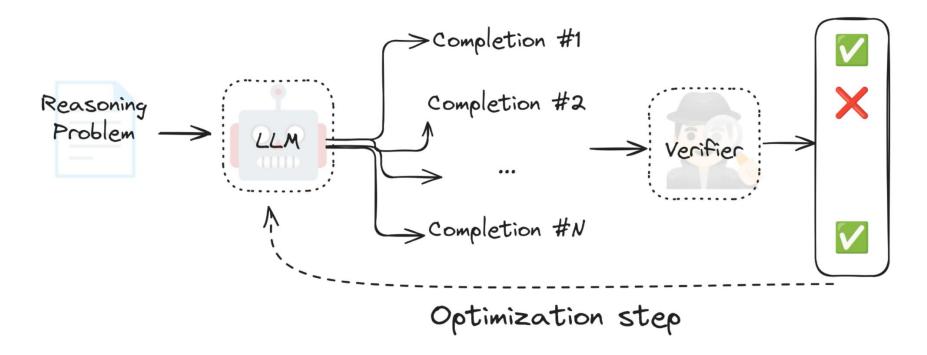
Congrats to DeepSeek on producing an o1-level reasoning model! Their research paper demonstrates that they've independently found some of the core ideas that we did on our way to o1.

7:11 PM · Jan 28, 2025 · **8.2M** Views

DeepSeek-R1: closing the gap

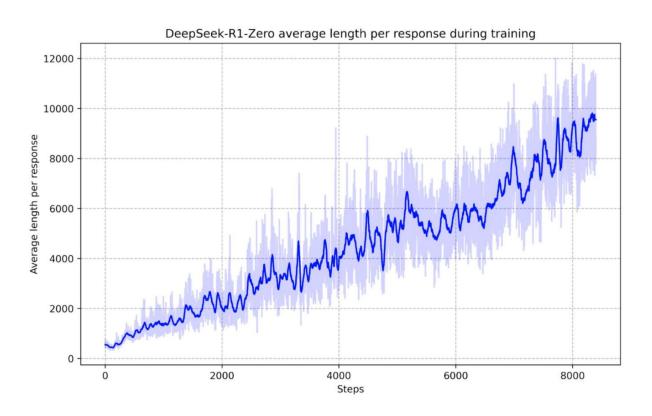


DeepSeek-R1: simpler than expected!



Reinforcement Learning with Verifiable Rewards (RLVR)

DeepSeek-R1: increased thinking time



DeepSeek-R1: "aha" moment

Question: If a > 1, then the sum of the real solutions of $\sqrt{a - \sqrt{a + x}} = x$ is equal to

Response: <think>

To solve the equation $\sqrt{a - \sqrt{a + x}} = x$, let's start by squaring both \cdots

$$\left(\sqrt{a-\sqrt{a+x}}\right)^2 = x^2 \implies a-\sqrt{a+x} = x^2.$$

Rearrange to isolate the inner square root term:

$$(a-x^2)^2 = a+x \implies a^2-2ax^2+(x^2)^2 = a+x \implies x^4-2ax^2-x+(a^2-a)=0$$

. . .

Wait, wait. Wait. That's an aha moment I can flag here.

Let's reevaluate this step-by-step to identify if the correct sum can be · · ·

We started with the equation:

$$\sqrt{a-\sqrt{a+x}}=x$$

First, let's square both sides:

$$a - \sqrt{a + x} = x^2 \implies \sqrt{a + x} = a - x^2$$

Next, I could square both sides again, treating the equation: · · ·

. . .

DeepSeek-R1: distillation into smol models

Model	AIME 2024		MATH-500	GPQA Diamond	LiveCode Bench	CodeForces
	pass@1	cons@64	pass@1	pass@1	pass@1	rating
GPT-40-0513	9.3	13.4	74.6	49.9	32.9	759
Claude-3.5-Sonnet-1022	16.0	26.7	78.3	65.0	38.9	717
OpenAI-o1-mini	63.6	80.0	90.0	60.0	53.8	1820
QwQ-32B-Preview	50.0	60.0	90.6	54.5	41.9	1316
DeepSeek-R1-Distill-Qwen-1.5B	28.9	52.7	83.9	33.8	16.9	954
DeepSeek-R1-Distill-Qwen-7B	55.5	83.3	92.8	49.1	37.6	1189
DeepSeek-R1-Distill-Qwen-14B	69.7	80.0	93.9	59.1	53.1	1481
DeepSeek-R1-Distill-Qwen-32B	72.6	83.3	94.3	62.1	57.2	1691
DeepSeek-R1-Distill-Llama-8B	50.4	80.0	89.1	49.0	39.6	1205
DeepSeek-R1-Distill-Llama-70B	70.0	86.7	94.5	65.2	57.5	1633

Can we train fully open reasoning models?

datasets, tooling, knowledge

The spectrum of open

closed model APIs

open model weights

fully open model

















closed

open

Open weights and open source

open weights:

- can be fine-tuned and aligned
- run locally or on provider
- data contamination
- no control for content creators
- reproducibility

open source:

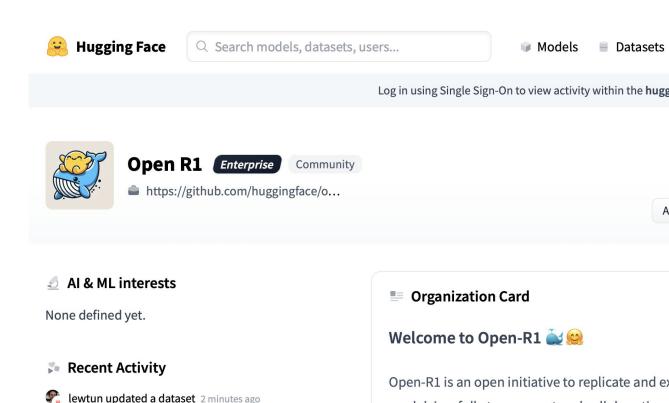
- data is available
- training code is available
- fosters innovation
- builds trust in the systems
- anybody can built on top

Open R1: fully reproduce DeepSeek-R1

open-r1/details-open-r1 R1-Distill-Owen-Math-...

Many details missing from DeepSeek-R1 tech report:

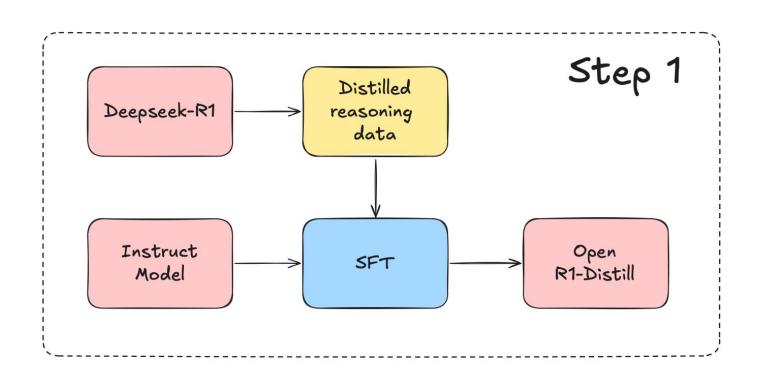
- Training code?
- Scaling and trade-offs??
- Verifiers???
- Data????



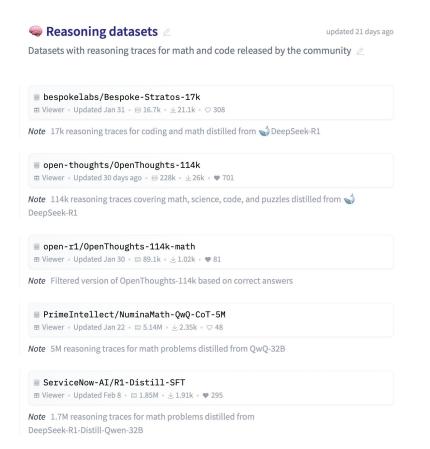
model, in a fully transparent and collaborative

https://huggingface.co/open-r1

Open R1: step 1 - distilled models



Distillation goes brr: math



Datasets 1.582 reasoning 8 Full-text search ↑↓ Sort: Trending FreedomIntelligence/medical-o1-reasoning-... ZennyKenny/synthetic_vc_financial_decisio... B Viewer • Updated 14 days ago • ■ 90.1k • ± 11.9k • ♥ 678 B Viewer • Updated about 17 hours ago • ■ 200 • ± 553 • ♡ 9 twinkle-ai/tw-function-call-reasoning-10k ZennyKenny/tactical-military-reasoning-v... Wiewer • Updated 11 days ago • ■ 150 • ± 560 • ♥ 6 ■ Viewer • Updated 6 days ago • ■ 10k • ↓ 188 • ♡ 5 nlpllmeval/NLP-Course-LLM-Reasoning-Eval-... twinkle-ai/tw-reasoning-instruct-50k B Viewer • Updated 3 days ago • ■ 918 • ± 114 • ♥ 5 B Viewer • Updated 7 days ago • ■ 50k • ± 179 • ♥ 4 AndriyBilinskiy/logical-reasoning-ua glaiveai/reasoning-v1-20m ■ Viewer • Updated Feb 6 • ■ 20k • ↓ 220 • ♡ 3 ■ Viewer • Updated Mar 19 • ■ 22.2M • ↓ 7.67k • ♥ 206 reedmavhew/claude-3.7-sonnet-reasoning twinkle-ai/tw-math-reasoning-2k ■ Viewer • Updated Mar 24 • ■ 179 • ↓ 396 • ♡ 7 ■ Viewer • Updated 7 days ago • ■ 2k • ± 100 • ♡ 2 albertvillanova/visual-spatial-reasoning moremilk/CoT Reasoning The Ancient Past ■ Viewer • Updated 6 days ago • ■ 6k • ± 42 • ♥ 2 Updated Dec 14, 2022 • ± 38 • ♥ 5

Math: finding hard problems



English (eng), day 1

Tuesday, 16. July 2024

Problem 1. Determine all real numbers α such that, for every positive integer n, the integer

$$\lfloor \alpha \rfloor + \lfloor 2\alpha \rfloor + \cdots + \lfloor n\alpha \rfloor$$

is a multiple of n. (Note that $\lfloor z \rfloor$ denotes the greatest integer less than or equal to z. For example, $\lfloor -\pi \rfloor = -4$ and $\lfloor 2 \rfloor = \lfloor 2.9 \rfloor = 2$.)

Problem 2. Determine all pairs (a,b) of positive integers for which there exist positive integers g and N such that

$$\gcd(a^n + b, b^n + a) = g$$

holds for all integers $n \ge N$. (Note that gcd(x, y) denotes the greatest common divisor of integers x and y.)

Problem 3. Let a_1, a_2, a_3, \ldots be an infinite sequence of positive integers, and let N be a positive integer. Suppose that, for each n > N, a_n is equal to the number of times a_{n-1} appears in the list $a_1, a_2, \ldots, a_{n-1}$.

Prove that at least one of the sequences a_1, a_3, a_5, \ldots and a_2, a_4, a_6, \ldots is eventually periodic.

(An infinite sequence b_1, b_2, b_3, \ldots is eventually periodic if there exist positive integers p and M such that $b_{m+p} = b_m$ for all $m \ge M$.)

Solution 1

To solve the problem, we need to find all real numbers α such that, for every positive integer n, the integer

$$S_n(\alpha) = \lfloor \alpha \rfloor + \lfloor 2\alpha \rfloor + \dots + \lfloor n\alpha \rfloor$$

is divisible by n, i.e., $S_n(\alpha) \equiv 0 \mod n$.

Step 1: Break Down lpha into Integer and Fractional Parts

Let lpha=m+f , where $m=\lfloor lpha
floor \in \mathbb{Z}$ and $f=\{lpha\} \in [0,1)$ is the fractional part of lpha.

Step 2: Express the Sum in Terms of m and f

Using this, we have:

$$|k\alpha| = |k(m+f)| = km + |kf|.$$

So, the sum becomes:

$$S_n(\alpha) = m \sum_{k=1}^n k + \sum_{k=1}^n \lfloor kf \rfloor = m \frac{n(n+1)}{2} + \sum_{k=1}^n \lfloor kf \rfloor.$$

Step 3: Modulo n Simplification

We are interested in $S_n(\alpha) \mod n$:

$$S_n(\alpha) \equiv \left(m \frac{n(n+1)}{2} + \sum_{k=1}^n \lfloor kf \rfloor \right) \mod n.$$

Since $m^{\frac{n(n+1)}{2}}$ is divisible by n, the expression simplifies to

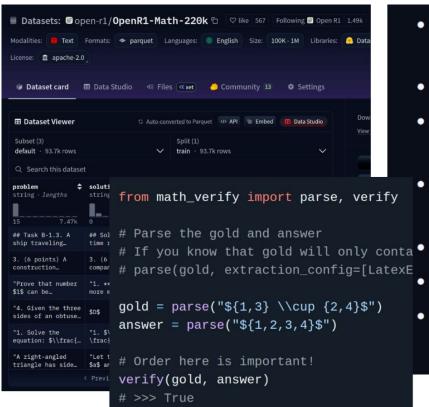
$$S_n(lpha) \equiv \sum_{k=1}^n \lfloor kf \rfloor \mod n.$$

Step 4: Analyze the Fractional Part f

Our goal is to find all $f \in [0,1)$ such that:

$$\sum_{k=1}^{n} \lfloor kf \rfloor \equiv 0 \mod n \text{ for all } n \in \mathbb{N}.$$

Math: verifying model answers

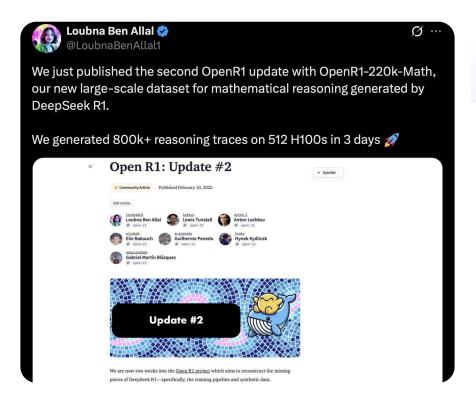


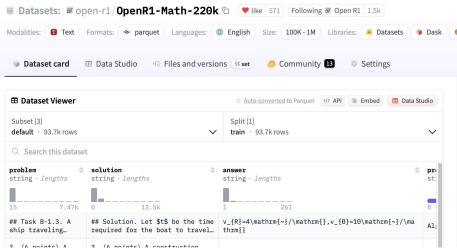
- Complete set theory support (Intervals, FiniteSets, set operations)
- Unicode symbol substituion support (e.g. β -> beta)
- Applies Latex fixes for common malformations (e.g. frac13 -> 1/3)
- Equation and inequality parsing, with symbol assignment resolution (e.g. x = 1 -> 1)
- Percentage best effort conversion (e.g. 10% -> 0.1)
- Units in text handling (e.g. 10 cm -> 10)
- Exact representation of the input expressions (e.g.

```
0.333 -> Float(333, 3)
```

https://github.com/huggingface/Math-Verify

Math: open data for model training





hf.co/datasets/open-r1/OpenR1-Math-220k

Distillation goes brr: code



HOME TOP CATALOG CONTESTS GYM PROBLEMSET GROUPS RATING EDU API CALENDAR HELP

PROBLEMS SUBMIT CODE MY SUBMISSIONS STATUS HACKS STANDINGS CUSTOM INVOCATION

D. Array and GCD

time limit per test: 2 seconds memory limit per test: 512 megabytes

You are given an integer array a of size n.

You can perform the following operations any number of times (possibly, zero):

- pay one coin and increase any element of the array by 1 (you must have at least 1 coin to perform this operation);
- gain one coin and decrease any element of the array by 1.

Let's say that an array is ideal if both of the following conditions hold:

- each element of the array is at least 2;
- for each pair of indices i and j ($1 \le i, j \le n$; $i \ne j$) the greatest common divisor (GCD) of a_i and a_j is equal to 1. If the array has less than 2 elements, this condition is automatically satisfied.

Let's say that an array is beautiful if it can be transformed into an ideal array using the aforementioned operations, provided that you initially have no coins. If the array is already ideal, then it is also beautiful.

The given array is not necessarily beautiful or ideal. You can remove any elements from it (including removing the entire array or not removing anything at all). Your task is to calculate the minimum number of elements you have to remove (possibly, zero) from the array a to make it beautiful.

inpu

The first line contains a single integer t ($1 \le t \le 10^4$) — the number of test cases.

The first line of each test case contains a single integer n ($1 \le n \le 4 \cdot 10^5$).

The second line contains n integers a_1, a_2, \ldots, a_n ($2 \le a_i \le 10^9$).

Additional constraint on the input: the sum of n over all test cases doesn't exceed $4 \cdot 10^5$.

Output

For each test case, print a single integer — the minimum number of elements you have to remove (possibly, zero) from the array a to make it **beautiful**.

Example	
input	Сору
5	
3 5 5 5	
4 2 3 2 4	
1 3	
3 2 100 2	
5 2 4 2 11 2	
output	Сору
0	
2	
0	
0 1	

Note

In the first example, you don't need to delete any elements, because the array is already beautiful. It can be transformed into an ideal array as follows: $[5,5,5] \rightarrow [4,5,5] \rightarrow [4,5,5] \rightarrow [4,3,5]$ (you end up with 3 coins).

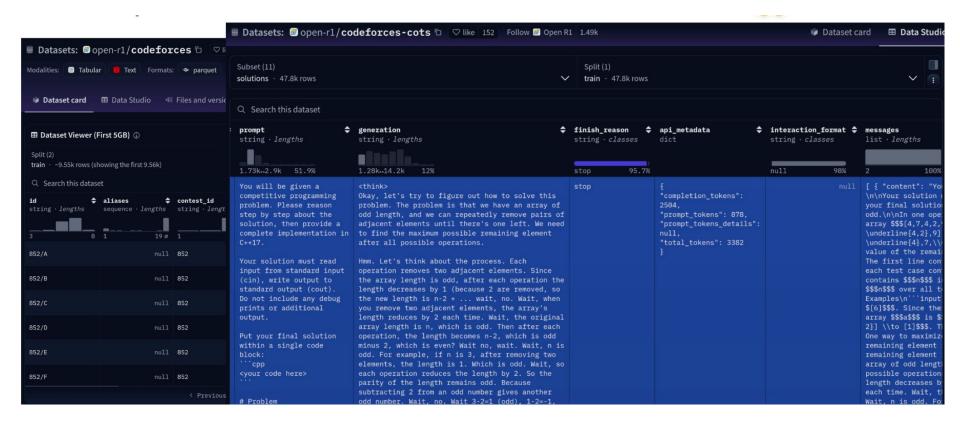
In the second example, you need to remove 2 elements so that the array becomes beautiful. If you leave the elements [2,3] and delete the other elements, then the given array is already ideal (and therefore, beautiful).

In the third example, you don't need to delete any elements because the array is already ideal (and thus, beautiful).

In the fourth example, the array is beautiful. It can be transformed into an ideal array as follows: $[2,100,2] \rightarrow [2,99,2] \rightarrow [2,99,3] \rightarrow [2,98,3] \rightarrow [2,97,3]$ (you end up with 2 coins).

Contest status							
#	When	Who	Problem	Lang	Verdict	Time	Memory
318205236	May/03/2025 12:07 ^{UTC+2}	23CS02002	D - Array and GCD	C++23 (GCC 14-64, msys2)	Running on test 15	0 ms	0 KB
318205233	May/03/2025 12:07 ^{UTC+2}	SajidZakaria 00:57	D - Array and GCD	C++20 (GCC 13-64)	Wrong answer on test 4	453 ms	134100 KB
318205003	May/03/2025 12:04 ^{UTC+2}	23CS02002	D - Array and GCD	C++23 (GCC 14-64, msys2)	Runtime error on test 4	406 ms	74800 KB
318205011	May/03/2025 12:04 ^{UTC+2}	Krityapriya	D - Array and GCD	C++23 (GCC 14-64, msys2)	Wrong answer on test 5	93 ms	7800 KB
318204841	May/03/2025 12:03 ^{UTC+2}	23CS02002	D - Array and GCD	C++23 (GCC 14-64, msys2)	Runtime error on test 4	202 ms	43500 KB
318204372	May/03/2025 11:57 ^{UTC+2}	RaduM 90:37	D - Array and GCD	C++17 (GCC 7-32)	Accepted	187 ms	5500 KB

Code: problem dataset & distillation



Code: OlympicCoder



101 2024 Ec

International Olympiad in Informatics (2024)

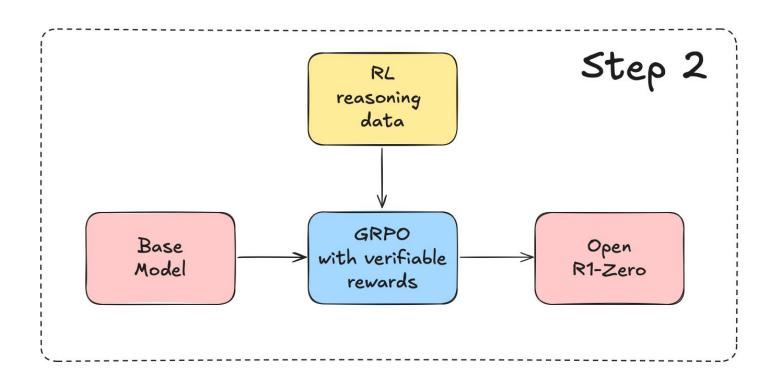
Performance of 10 selected models across 50 submissions

Practice Tasks

- aplusb
 - Statement: Official English
 - Task attachments
 - Test data
- machine
 - O Statement: Official English
 - Task attachments
 - Test data
- pyramids
 - O Statement: Official English
 - Task attachments
 - Test data
- treasure
 - O Statement: Official English
 - Task attachments



Open R1: step 2 - RL with verifiable rewards



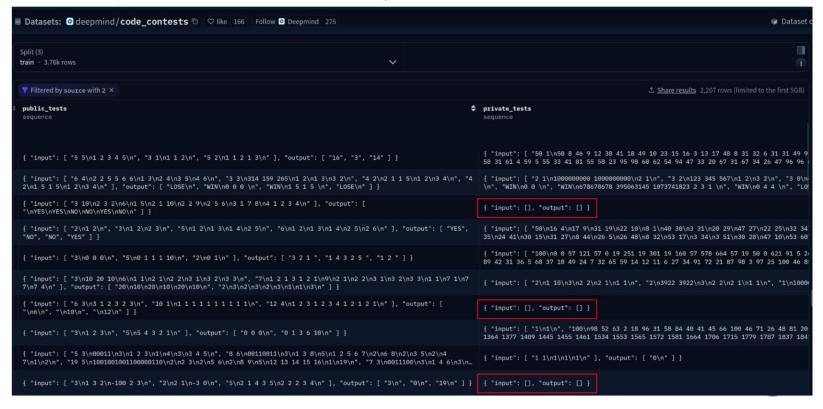
TRL: reinforcement learning for LLMs



```
GRPOTrainer
GRPOTrainer implements the Group Relative Policy
Optimization (GRPO) algorithm that is more memory-
efficient than PPO and was used to train Deepseek AI's R1.
 from datasets import load_dataset
 from trl import GRPOTrainer
 dataset = load_dataset("trl-lib/tldr", split="tr-
 # Dummy reward function: count the number of uni-
 def reward_num_unique_chars(completions, **kwarg
     return [len(set(c)) for c in completions]
 trainer = GRPOTrainer(
     model="Owen/Owen2-0.5B-Instruct",
     reward_funcs=reward_num_unique_chars,
     train_dataset=dataset,
 trainer.train()
```

Code verifiability crisis

"verifiable" problems with weak tests only



Code verifiability crisis

Problem	Lang	Verdict	Time	Memory			
1246E - To Make 1	PyPy 3-64	Wrong answer on test 4	93 ms	0 KB			
1148G - Gold Experience	PyPy 3-64	Wrong answer on test 14	687 ms	124500 KB			
1148H - Holy Diver	PyPy 3-64	Time limit exceeded on test 26	3000 ms	72600 KB			
1515H - Phoenix and Bits	PyPy 3-64	Time limit exceeded on test 7	4000 ms	65400 KB			
1056H - Detect Robots	PyPy 3-64	Wrong answer on test 3	77 ms	0 KB			
1515H - Phoenix and Bits	Python 3	Time limit exceeded on test 7	4000 ms	59600 KB			
1491I - Ruler Of The Zoo	Python 3	Wrong answer on test 4	406 ms	900 KB			

Code verifiability crisis



2025-01-06

CODEELO: Benchmarking Competition-level Code Generation of LLMs with Human-comparable Elo Ratings

B. Replace Character

time limit per test: 1 second memory limit per test: 256 megabytes

You're given a string s of length n, consisting of only lowercase English letters.

You must do the following operation exactly once:

- Choose any two indices i and j ($1 \le i, j \le n$). You can choose i = j.
- Set $s_i := s_j$.

You need to minimize the number of distinct permutations of s. Output any string with the smallest number of distinct permutations after performing exactly one operation.

† A permutation of the string is an arrangement of its characters into any order. For example, "bac" is a permutation of "abc" but "bcc" is not.

Input

Each test contains multiple test cases. The first line contains the number of test cases t ($1 \le t \le 500$). The description of the test cases follows.

The first line of each test case contains n ($1 \le n \le 10$) — the length of string s.

A clear indication that needs a special judge

The second line of each test case contains s of length n. The string contains only lowercase English letters.

Output

For each test case, output the required s after applying exactly one operation. If there are multiple solutions, print any of them.

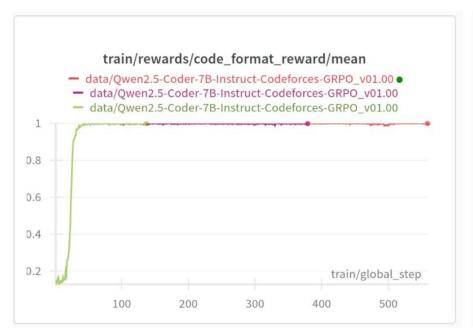
~30% require a special checker

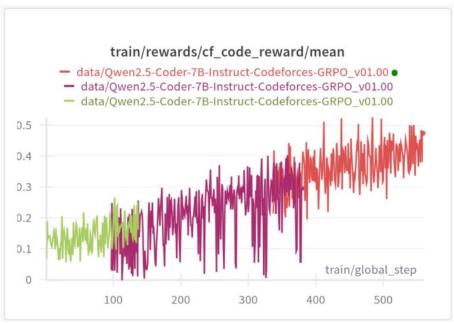
R1 generated checkers working for 60%+ of them

Validated with correct and incorrect solutions

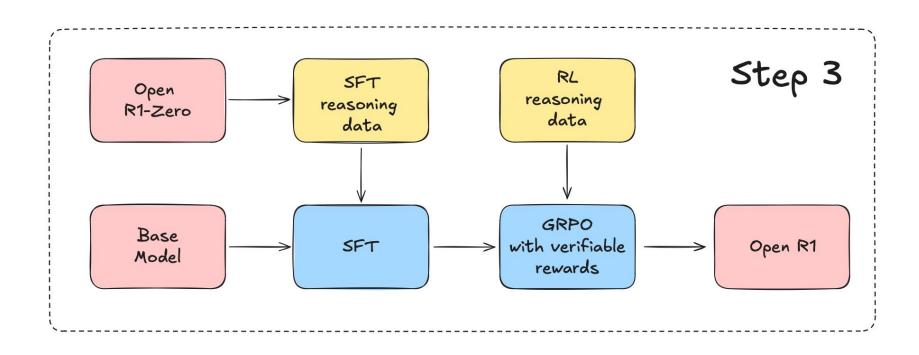
-> Apply same idea to test cases

Code reward curves





Open R1: step 3 - bring it altogether (WIP)



What impact has DeepSeek-R1 had on open AI?

DeepSeek-R1: huge impact on open Al!

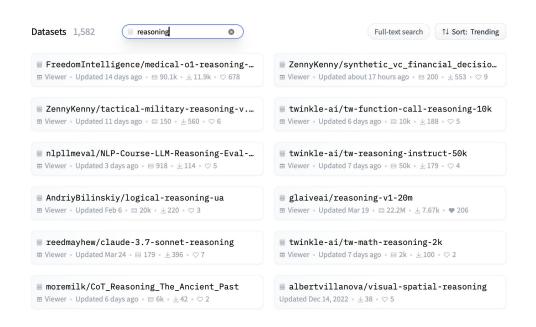






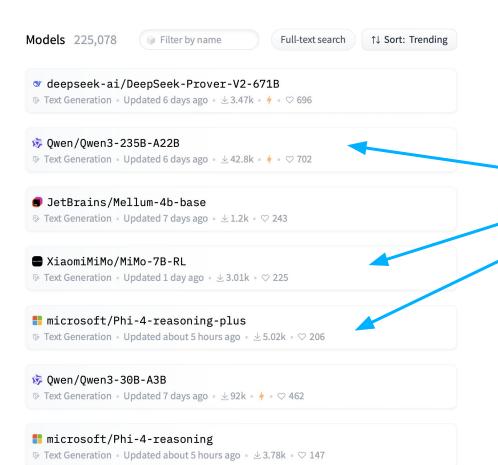
We now have much better tools for reinforcement learning 6

DeepSeek-R1: huge impact on open Al!



1000+ reasoning datasets now available, with large orgs like NVIDIA also contributing

DeepSeek-R1: huge impact on open Al!



Reasoning models now available in many shapes and sizes

Thank you!



